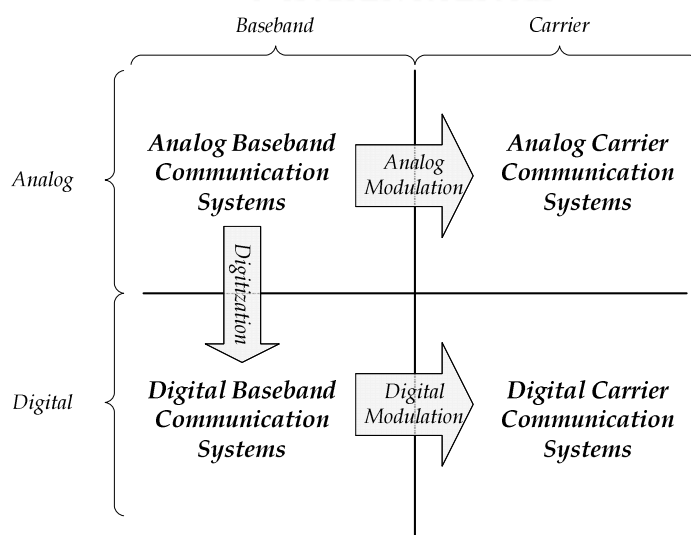


Lecture 5a: Sampling and Quantization

Prof. Mohammed Hawa
Electrical Engineering Department
The University of Jordan

EE421: Communications I

Digitization



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2

Digital Systems Advantages

- Immunity to noise (threshold detection; regenerative repeaters).
- Multiplexing at the baseband level (e.g., TDM) and carrier level (e.g., CDMA and OFDMA).
- Spread spectrum techniques and orthogonality.
- Channel coding (i.e., error correcting codes).
- Source coding techniques (i.e., compression). *Also Encryption.*
- Exchanging SNR for bandwidth.
- Using microprocessors and DSP.
- Digital signal storage is relatively easy and inexpensive.



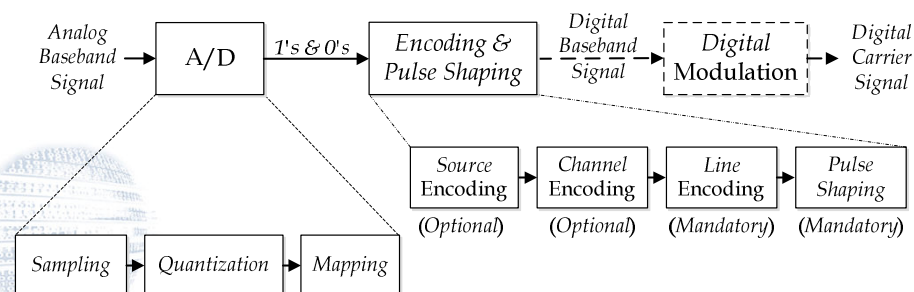
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Digitization

- **Sampling** (discrete analog signal).
- **Quantization** (quantized discrete signal)
- **Mapping** (stream of 1's and 0's).
- **Encoding and Pulse Shaping** (digital baseband signal).

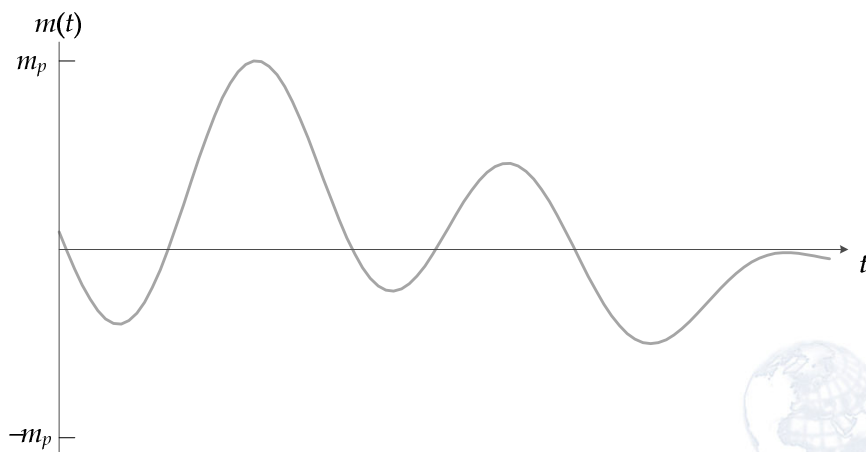


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Analog Signal

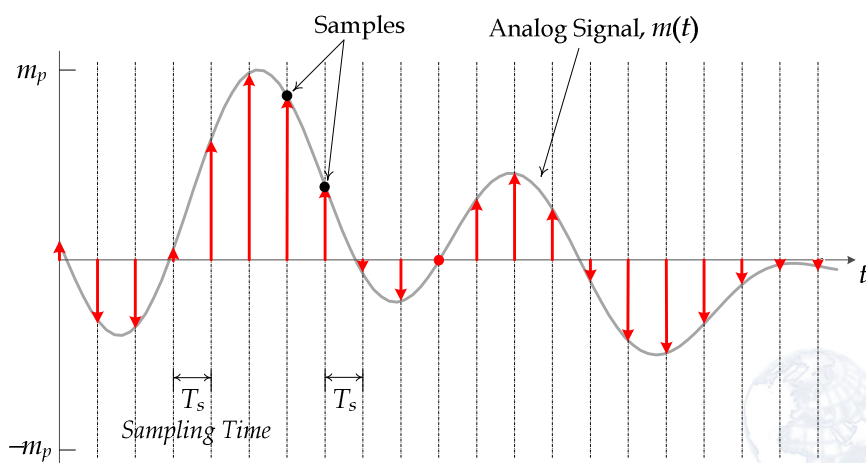


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Ideal Sampling

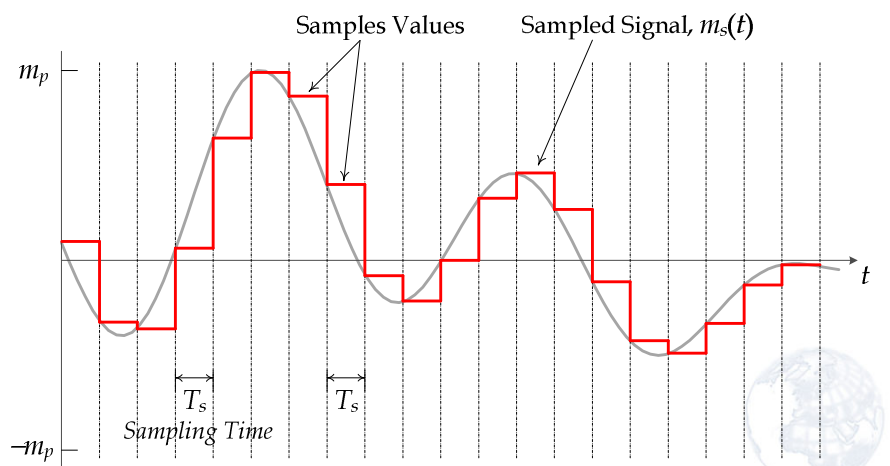


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Practical Sampling

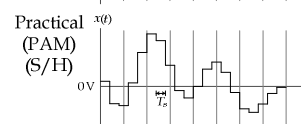
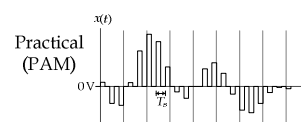
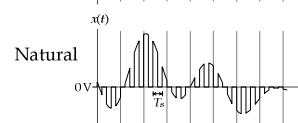
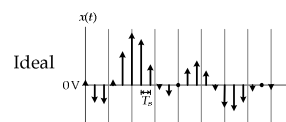
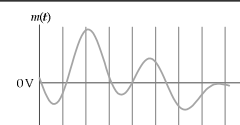
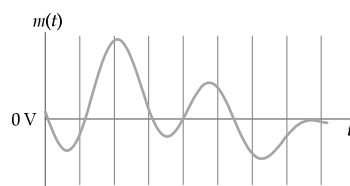


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7

Sampling

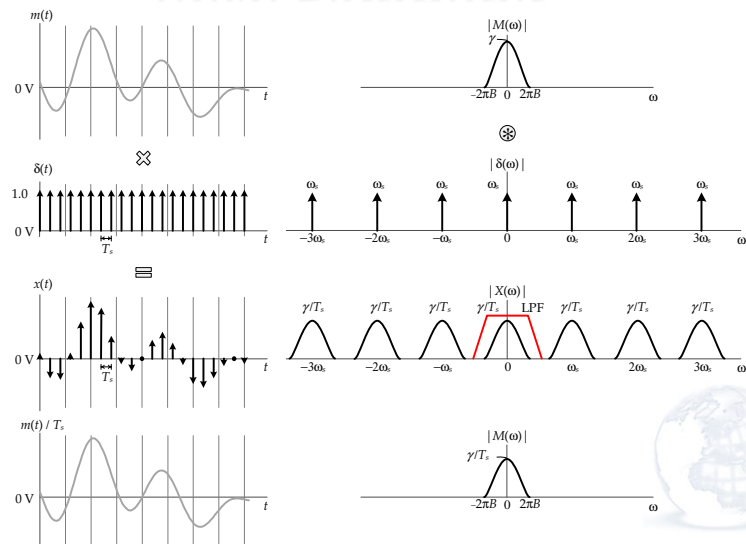


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8

Ideal Sampling

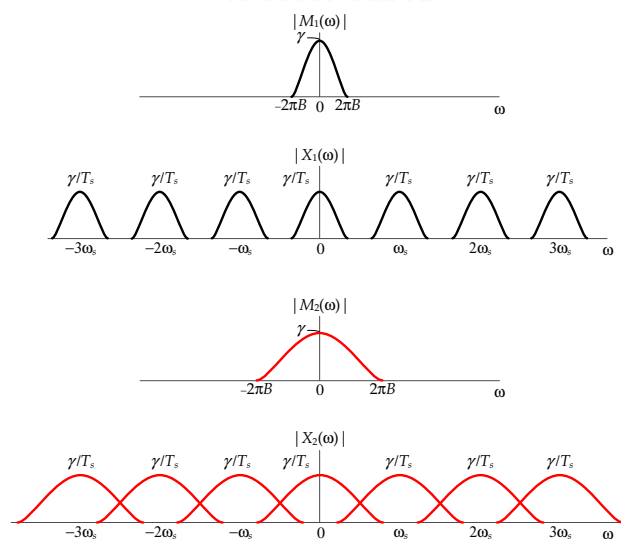


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Aliasing

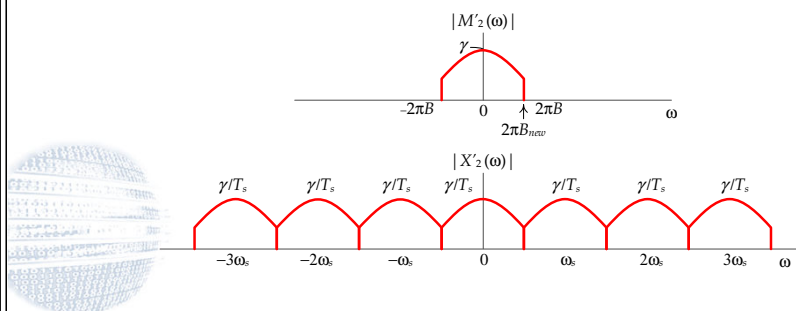
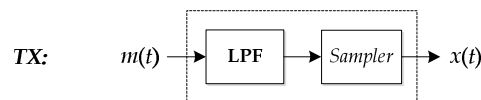


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Anti-Aliasing Filter

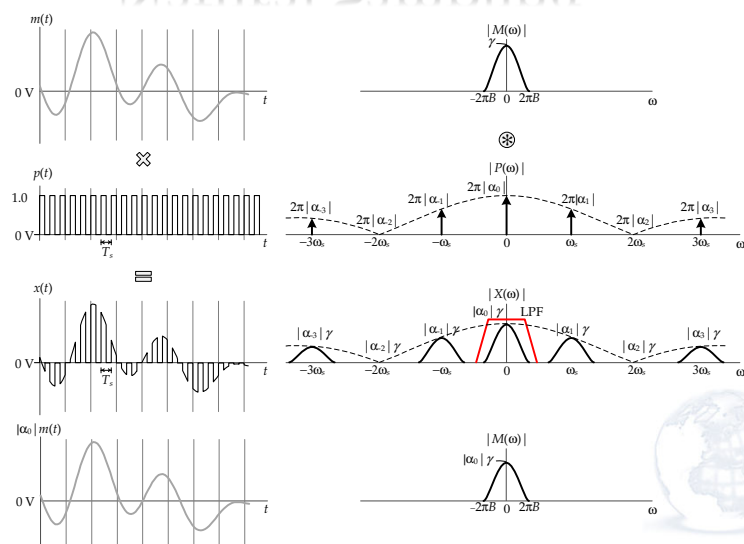


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11

Natural Sampling

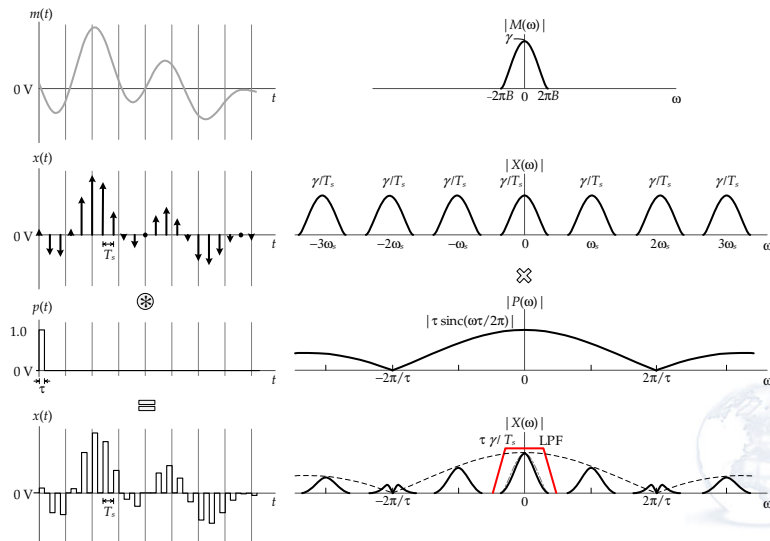


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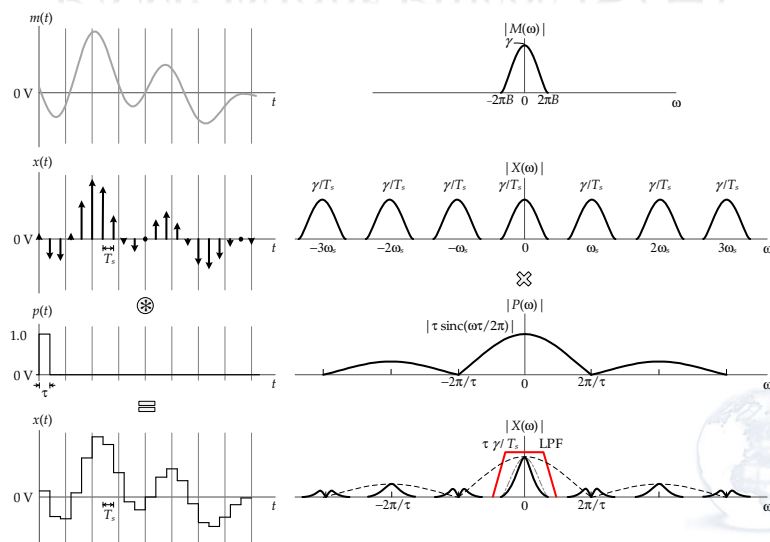
12

Practical Sampling: PAM



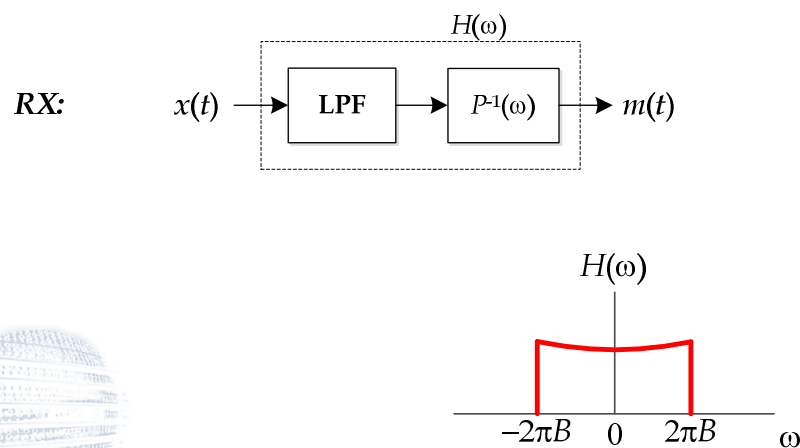
13

PAM: Wider Pulses (S/H)



14

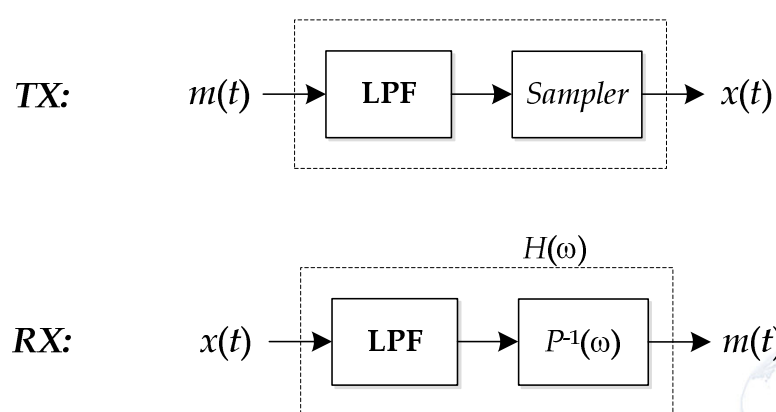
Distortion solved by Equalizer



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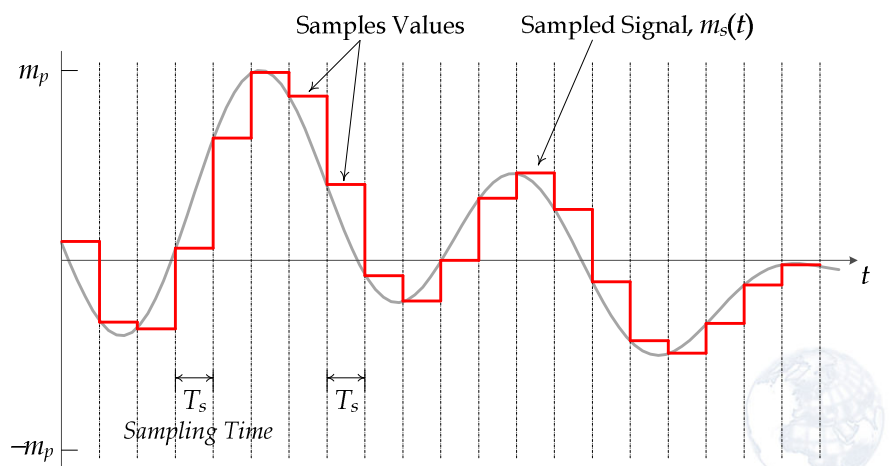
Summary



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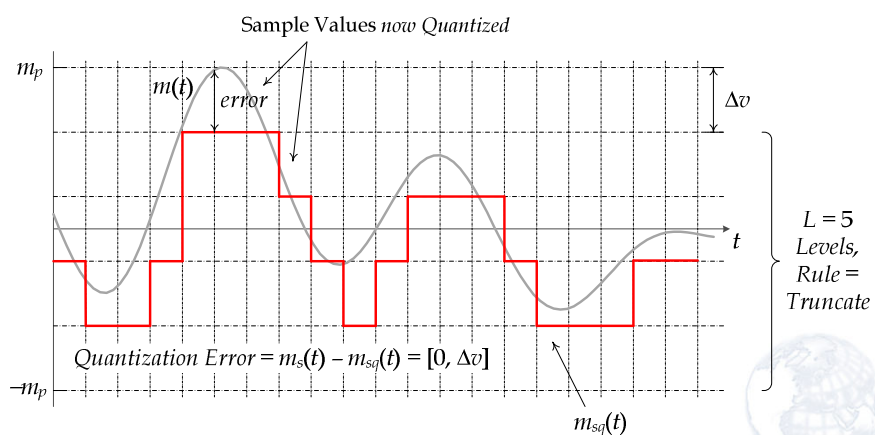
After Sampling!



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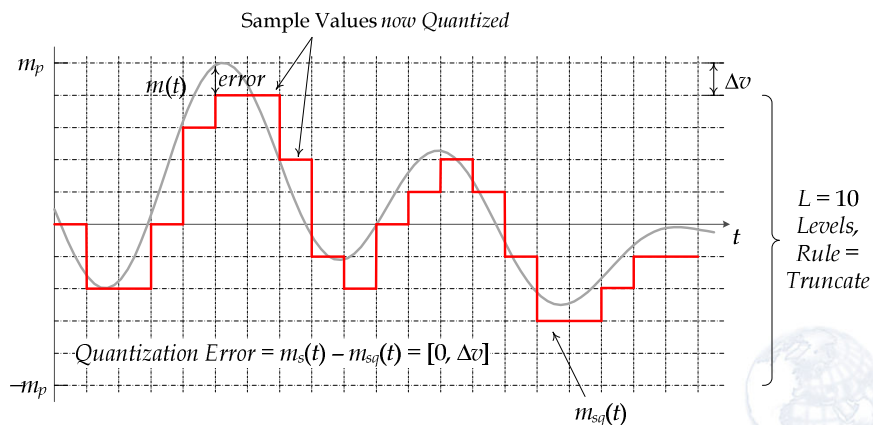
Quantization ($L = 5$)



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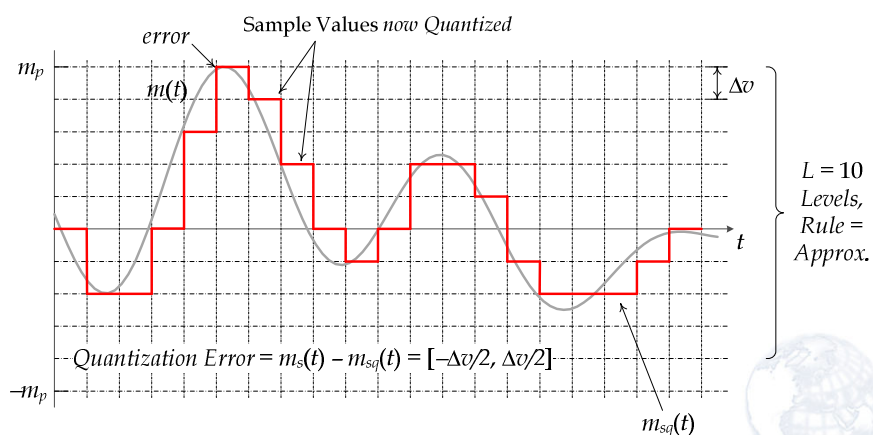
Quantization ($L = 10$)



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Quantization (Approx.)



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$L = 4$ versus $L = 8$

Levels, $L = 4$ (2 bits/sample)

$2.3333... \text{ V} \rightarrow$
 $3.0 \text{ V} \quad 11$
 $2.0 \text{ V} \quad 10 \rightarrow 10$
 $1.0 \text{ V} \quad 01$
 $0.0 \text{ V} \quad 00$
 $0.3333... \text{ V}$
Quantization Error

Rule: Approximate

Levels, $L = 8$ (3 bits/sample)

$2.3333... \text{ V} \rightarrow$
 $3.5 \text{ V} \quad 111$
 $3.0 \text{ V} \quad 110$
 $2.5 \text{ V} \quad 101 \rightarrow 101$
 $2.0 \text{ V} \quad 100$
 $1.5 \text{ V} \quad 011$
 $1.0 \text{ V} \quad 010$
 $0.5 \text{ V} \quad 001$
 $0.0 \text{ V} \quad 000$
 $0.1666... \text{ V}$
Quantization Error

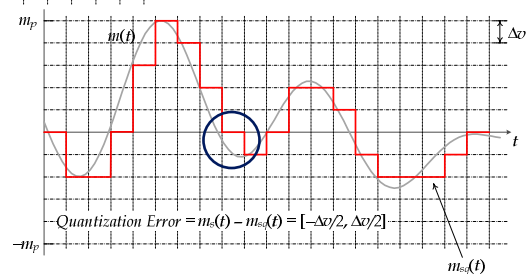
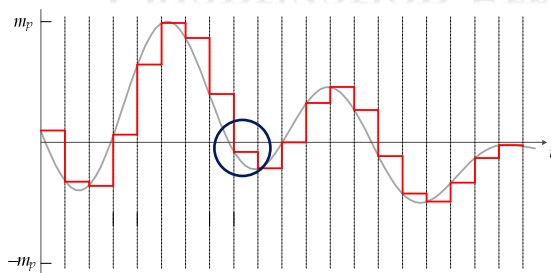


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21

Quantization Error $\approx$ Noise



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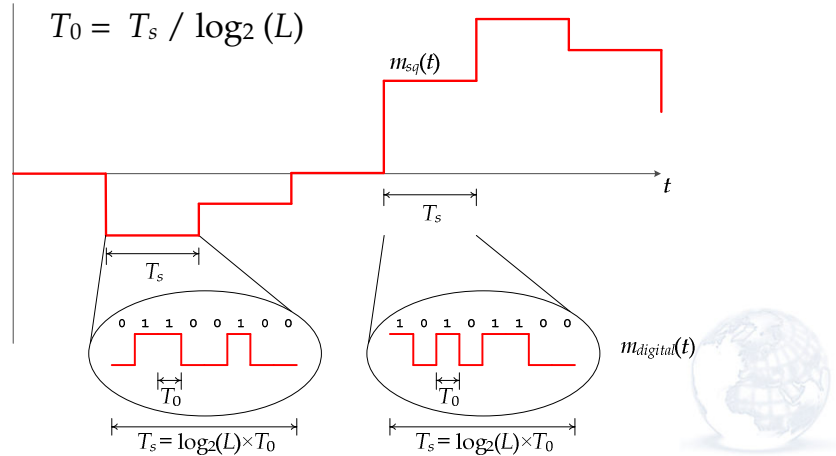
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22

Mapping

$$f_0 \text{ [bps]} = f_s \text{ [samples/s]} \times \log_2(L) \text{ [bits/sample]}$$

$$T_0 = T_s / \log_2(L)$$



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Source Coding



0000	00
0001	01
0010	1000
0011	1001
0100	1010
0101	1011
0110	110000
0111	110001
1000	110010
1001	110011
1010	110100
1011	110101
1100	110110
1101	110111
1110	111000
1111	111001

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Audio Compression

- Landline telephony (PCM, no compression)
 - **64 kbps**
- Linear Prediction Coding (LPC) vocoder
 - e.g., RPE-LTP (regular pulse excitation, long-term prediction) LPC codec (GSM cellular phones, Full Rate): **13 kbps**.
- Code-Excited linear Prediction (CELP) vocoder
 - Algebraic CELP(ACELP) (GSM cellular phones, Enhanced Full Rate): **12.2 kbps**
 - FS-1016 (United States Department of Defense): **4.8 kbps**

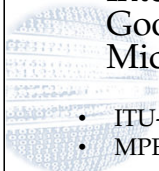


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Video Compression

- **MPEG-2 (ITU-T H.222/H.262)**: DVDs and Digital TV broadcasting.
 - **ITU-T H.264 / MPEG-4 Part 10** or AVC (Advanced Video Coding): Almost everything.
 - **ITU-T H.265 / MPEG-H Part 2** or HEVC (High Efficiency Video Coding): Powerful. Expensive!
 - **AV1** (AOMedia Video 1): open, royalty-free, designed for video transmissions over the Internet. High compression ratio. Supported by Google, Facebook, Apple, Cisco, IBM, Intel, Microsoft, Netflix, Nvidia, etc.
- ITU-T: International Telecommunication Union - Telecommunication
 - MPEG: Moving Picture Experts Group



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Channel Coding

111001010111010001010100

→ 111001010111010001010100**1011**

→ 1110010101~~0~~1010001010100**1011**

→ 111001010111010001010100



$$C = B_{ch} \times \log_2(1 + SNR)$$